

# Measurement of Little Higgs Parameters at International Linear Collider

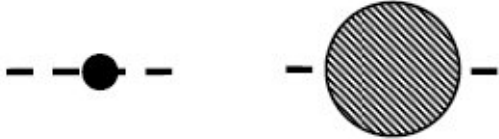
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# Little hierarchy problem

There are two predictions of the energy scale for new physics ( $\Lambda$ ).

- $\Lambda < 1 \text{ TeV}$  :  $<10\%$  fine tuning of Higgs mass.
- $\Lambda > 10 \text{ TeV}$  : EW precision measurements
  - The global fit of the EW parameters.  
( $\Gamma_Z$ ,  $M_W/M_Z$ ,  $\sin^2\theta_W$ , ...)



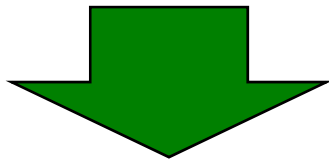
The diagram shows two Feynman diagrams representing quantum corrections to the Higgs mass. The first diagram on the left shows a dashed line with a solid black circle in the middle, representing a fermion loop. The second diagram on the right shows a dashed line with a shaded circle in the middle, representing a scalar loop.

$$m_h^2 = m_0^2 + \Lambda^2$$

Arrows from  $m_0^2$  and  $\Lambda^2$  point to  $100^2$  and  $1000^2$  respectively, with a double-headed arrow between them.

$$100^2 \Leftrightarrow 1000^2$$

→ There is a discrepancy between two predictions.



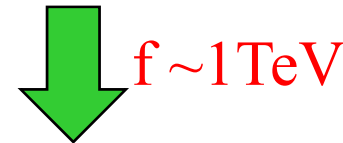
Some physics models are proposed to solve little hierarchy problem.

→ **Little Higgs model (with T-parity)**

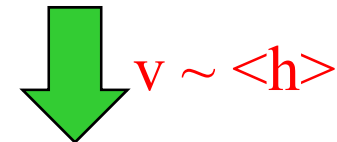
# Little Higgs mechanism

- Higgs is a pseudo NG boson of a global symmetry of SU(5) .
- The symmetry breaks to SO(5) at  $\Lambda \sim 10$  TeV.
  - VEV:  $f \sim 1\text{TeV}$
  - $[\text{SU}(2)_L \times \text{U}(1)_Y]$  is a subgroup of SO(5).
- The little Higgs partners contribute to cancel quadratic divergent term of  $M_h$  at 1-loop level.
  - The new physics at 1 TeV is not necessary.

$$\text{SU}(5): [\text{SU}(2) \times \text{U}(1)]^2$$



$$\text{SO}(5): \text{SU}(2)_L \times \text{U}(1)_Y$$



$$\text{U}(1)_Y$$

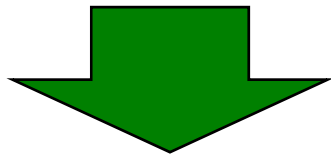
→ Little hierarchy problem can be solved.

The diagram shows two Feynman diagrams representing the cancellation of quadratic divergences in the Higgs mass. The first diagram is a top quark loop with external Higgs lines, labeled  $\Lambda_{\text{SM}}$ . The second diagram is a top quark loop with a top partner  $T$  loop, labeled  $\Lambda_{\text{NP}}$ . The sum of these two diagrams is zero.

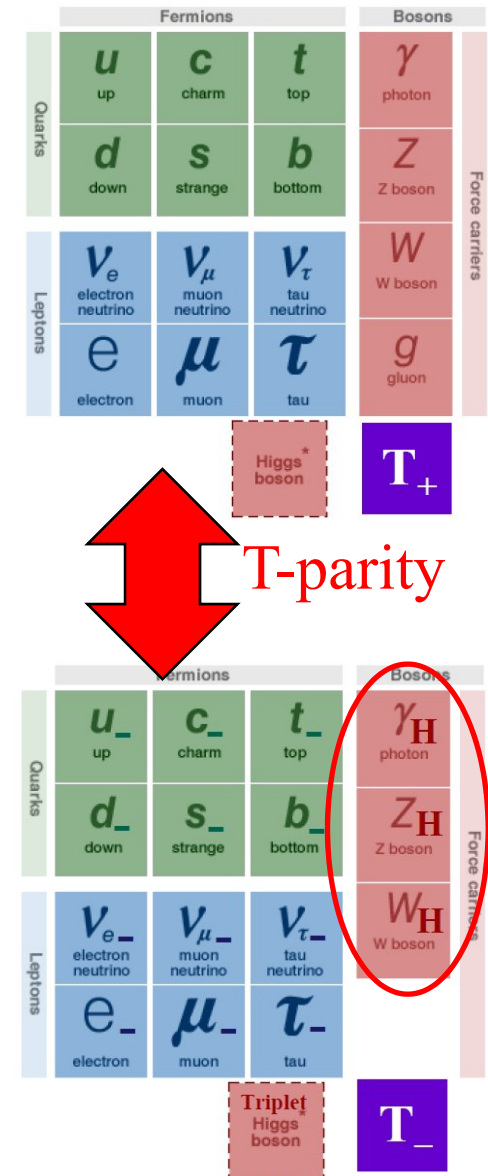
# Importance of heavy gauge bosons

## Heavy gauge bosons

- The heavy gauge bosons appears as the little Higgs partners of SM gauge bosons.
    - $\gamma, Z, W \leftrightarrow A_H, Z_H, W_H$
    - The masses have information of  $VEV(f)$ .
  - $A_H$  becomes stable, requiring T-parity.
    - $A_H$  is a dark matter candidate.
- **VEV and abundance of the dark matter can be evaluated by measurement of heavy gauge bosons.**



**Sensitivity of ILC to the heavy gauge bosons was studied.**

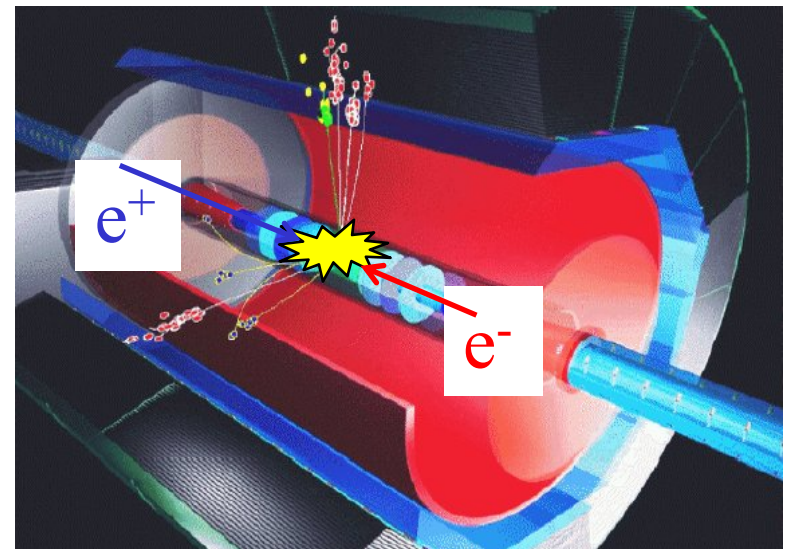
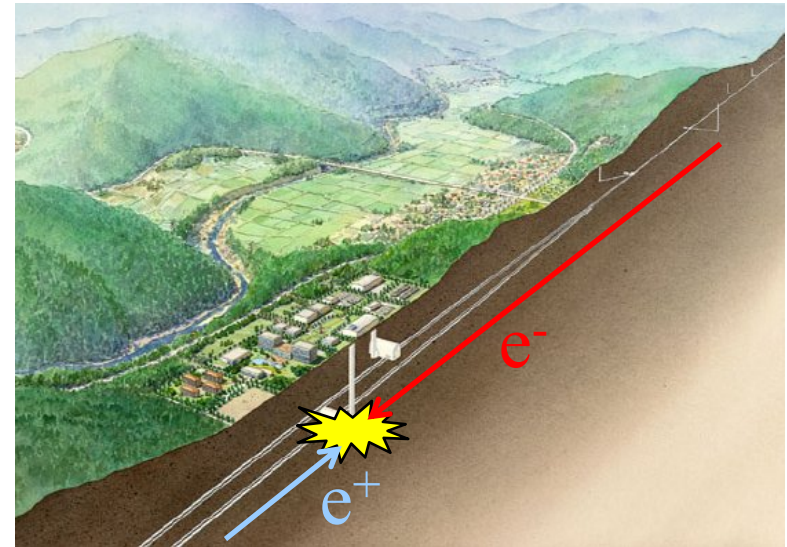


# International Linear Collider

## International Linear Collider (ILC)

- The future linear accelerator for  $e^+$  and  $e^-$ .
  - Total length:  $\sim 30\text{km}$
- $E_{\text{CM}}$ : **500 GeV in the first stage**
  - **1 TeV in the second stage**
- Luminosity:  $2 \times 10^{34} \text{ cm}^{-2}\text{s}^{-1}$
- Higgs and new physics will be studied at clean environment.
- R&D has been continued to establish the technology by 2012.

The simulation study was done for  $E_{\text{CM}} = 500\text{GeV}$  and 1 TeV.



# Parameter choice for simulation study

## Constraint by WMAP result

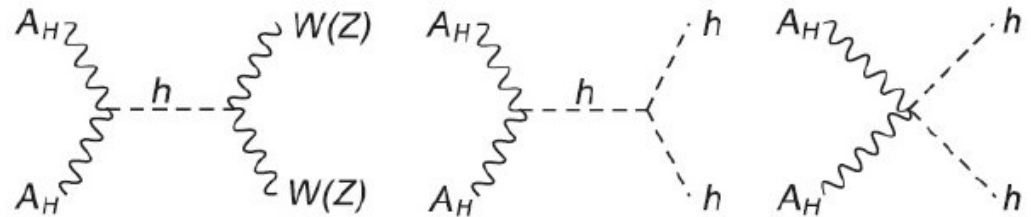
- The dark matter density was determined by WMAP.
  - $\Omega h^2 = 1.119 \pm 0.009$
- Annihilation xsec of  $A_H \sim F(M_h, f)$ 
  - $M_h$  and  $f$  are restricted by  $\Omega h^2$ .

## Parameters for this study

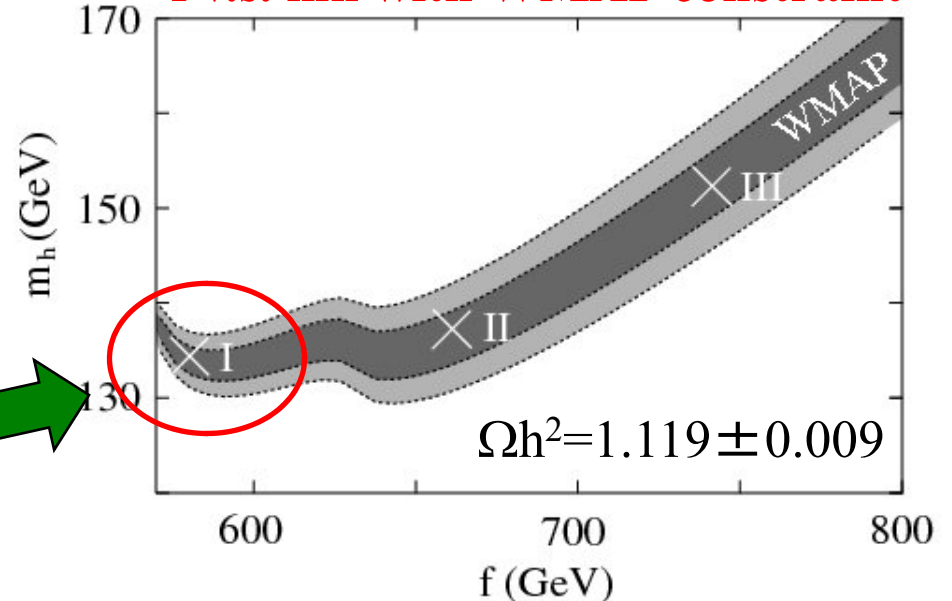
- $f$ : 580 GeV
- $M_h$ : 134 GeV
- $M_{A_H}$ : 81.9 GeV
- $M_{W_H}$ : 368 GeV
- $M_{Z_H}$ : 369 GeV

$A_H$ ,  $W_H$ , and  $Z_H$  can be observed at ILC.

## Annihilation processes of $A_H$



## $f$ v.s. $m_h$ with WMAP constraint

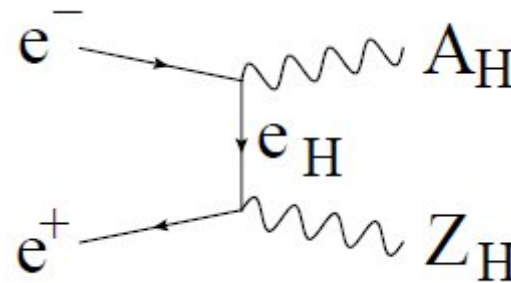


# Analysis modes

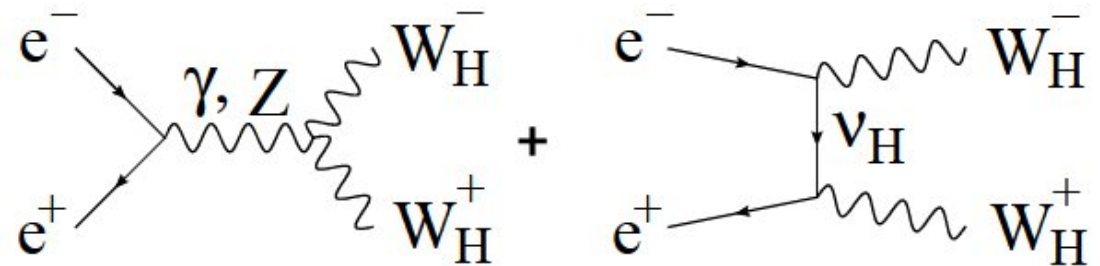
According to the beam energy at ILC, two analysis modes were selected.

## Analysis modes

- $A_H + Z_H$  @  $E_{CM} = 500$  GeV
  - xsec: 1.91 fb
  - $Z_H \rightarrow H + A_H$
  - $M_{A_H} + M_{Z_H} = 450.9$  GeV



- $W_H^+ + W_H^-$  @  $E_{CM} = 1$  TeV
  - xsec: 277 fb
  - $W_H \rightarrow W + A_H$
  - $M_{W_H} + M_{W_H} = 736$  GeV

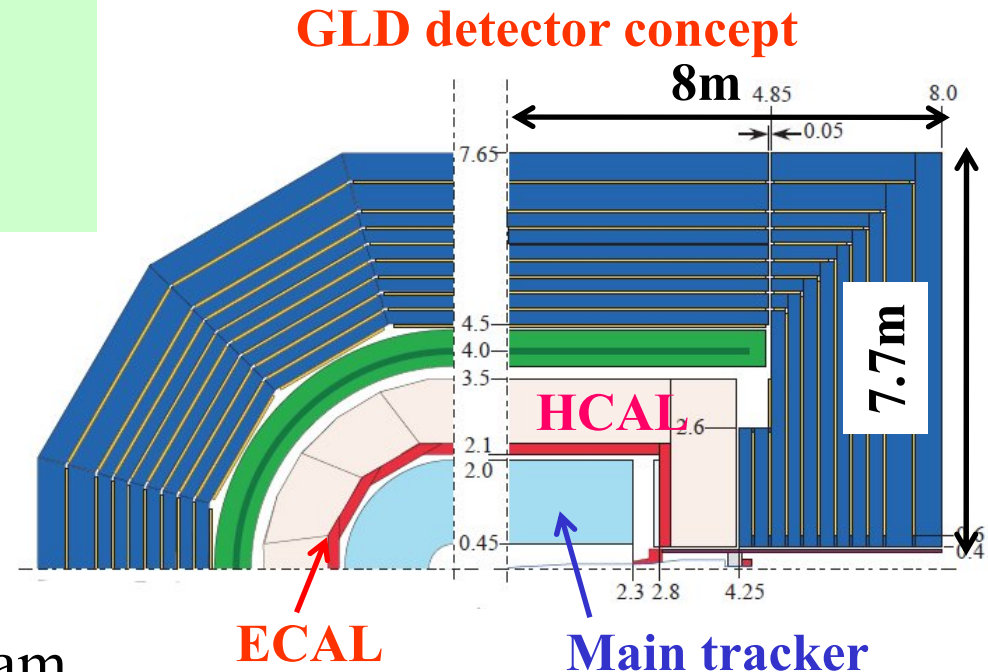




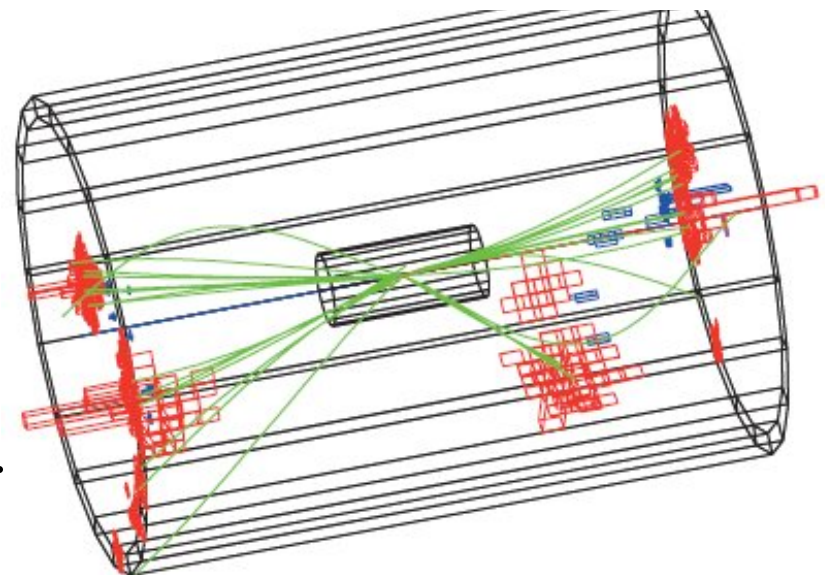
# Simulation study

## Simulation condition

- Event generator
  - Signal: PhysSim
  - BG: MadGraph and PhysSim
- ISR, FSR, beamstrahlung, and beam energy spread:
  - $E_{CM}=500\text{GeV}$ : not considered.
  - $E_{CM}=1\text{TeV}$ : considered.
- The fast-simulator for GLD was used.
  - The detector performance is included properly.
  - GLD was now re-organized as ILD.



## **Event display of a $W_H W_H$ event**



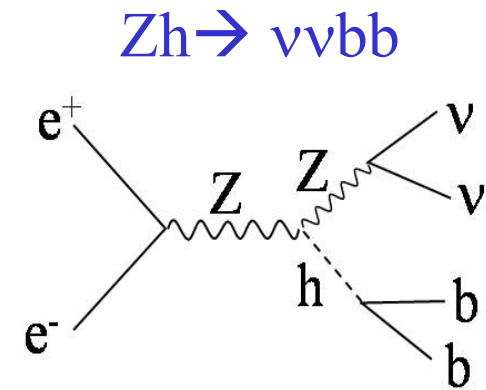
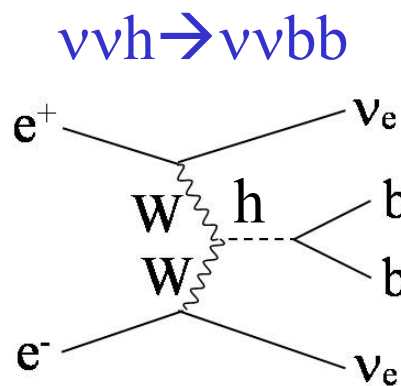
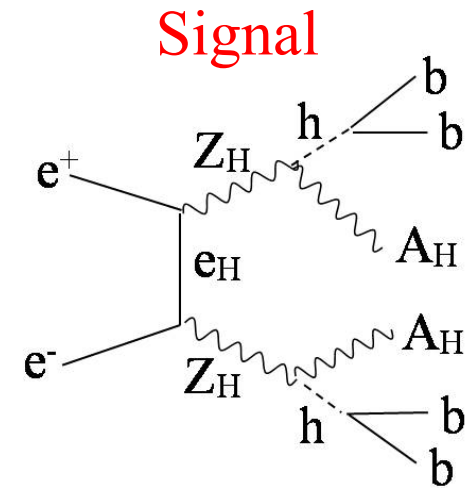


$A_H Z_H$  at  $E_{CM}=500\text{GeV}$

# Signal v.s. B.G. at $E_{CM}=500\text{GeV}$

## Signal v.s. BG

- Signal:  $A_H Z_H \rightarrow A_H A_H h h$  ( $h \rightarrow bb$ )
  - Xsec: 1.05fb
  - BR( $h \rightarrow bb$ ): 55.3% for  $M_h=134\text{GeV}$
- BG:  $\nu\nu h$  and  $Zh$  are serious BG.
  - $\nu\nu h \rightarrow \nu\nu bb$ : 34fb
  - $Zh \rightarrow \nu\nu bb$ : 5.57fb
- The selection cut was applied.
  - $100\text{GeV} < M_h < 140\text{GeV}$
  - $p_t^{\text{miss}} > 80\text{GeV}/c$
  - b-tagging



The number of events after the selection cut was checked.

# Event selection at $E_{\text{CM}}=500\text{GeV}$

## Event selection

- Assumption of b-tag performance
  - 80% efficiency for b-jet
  - 10% mis-identification of light quarks

• **Signal significance: 3.7**

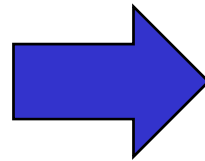
➔ **We will obtain the indication of new physics at  $E_{\text{CM}}=500\text{GeV}$ .**

Process	xsec(fb)	No cut	$100 < m_h < 140$	$P_t^{\text{miss}} > 80$	b-tag
$A_H Z_H \rightarrow A_H A_H b\bar{b}$	1.05	525	488	425	272
$\gamma Z \rightarrow \gamma b\bar{b}$	1,200	600,000	19,296	70	45
$tt \rightarrow W^+ W^- b\bar{b}$	496	248,000	859	413	264
$\nu\nu Z \rightarrow \nu\nu b\bar{b}$	44.3	22,150	635	261	167
$\nu\nu h \rightarrow \nu\nu b\bar{b}$	34.0	17,000	15,170	5,247	3,359
$ZZ \rightarrow \nu\nu b\bar{b}$	25.5	12,750	404	277	178
$Zh \rightarrow \nu\nu b\bar{b}$	5.57	2,785	2,390	2,196	1,406
<b>Total</b>		860,105	38,727	8,464	5,419

# Determination of $A_H$ & $Z_H$ mass

Masses of  $A_H$  and  $Z_H$  are determined by the edge of  $E_h$  distribution.

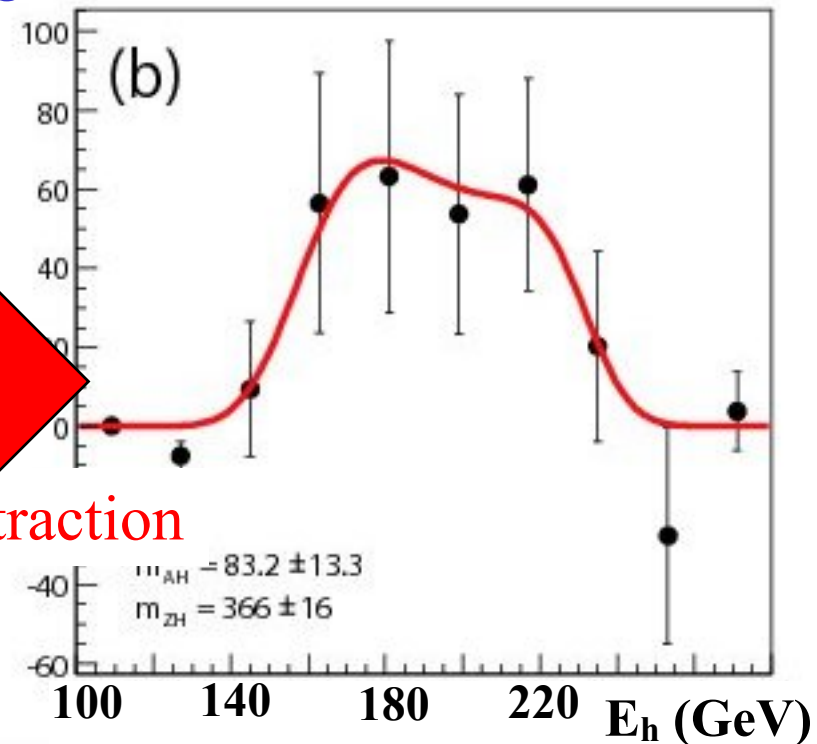
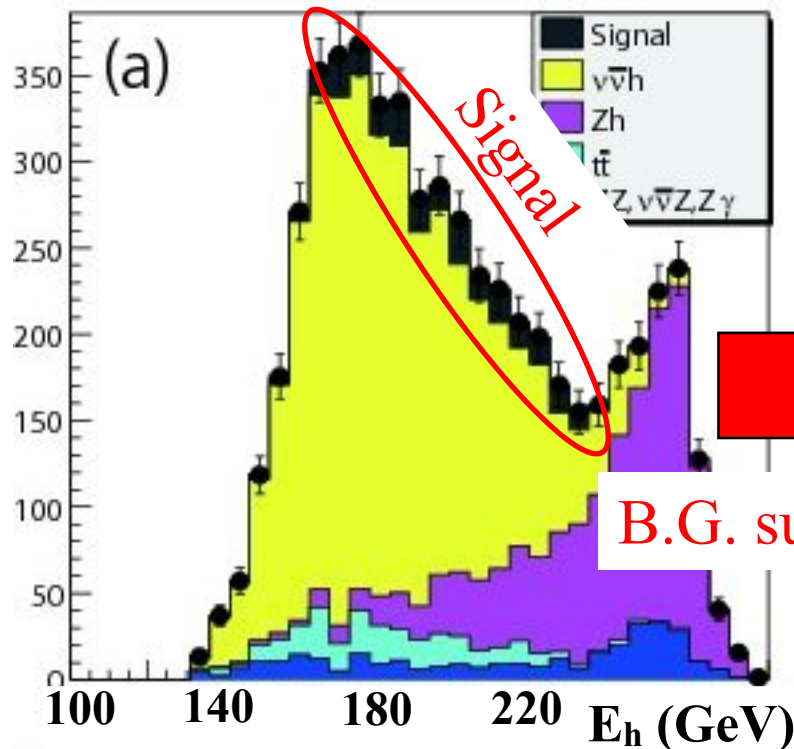
- $M_{A_H} : 83.2 \pm 13.3$  GeV
- $M_{Z_H} : 366.0 \pm 16.0$  GeV



Measurement accuracy

- $M_{A_H} : 16.2\%$
- $M_{Z_H} : 4.3\%$

Masses of  $A_H$  and  $Z_H$  might be determined at  $E_{CM}=500$ GeV.



$W_H W_H$  at  $E_{CM}=1\text{TeV}$

# Event selection at $E_{CM}=1\text{TeV}$

- Xsec of  $W_H W_H$  is very large, comparing to the SM background.
- The hadronic decay modes of W was selected as the signal.
  - $W_H W_H \rightarrow A_H A_H W W \rightarrow A_H A_H q q q q$
- SN of 4.2 was obtained with simple selection cuts.
- ➔ **The confident signal significance will be obtained at  $E_{CM}=1\text{TeV}$ .**

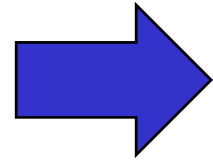
	Xsec(fb)	No cut	$E_W < 500\text{GeV}$	$\chi^2 < 26$	$p_T^{\text{miss}} > 84\text{GeV}$
$W_H W_H \rightarrow A_H A_H q q q q$	106.5	53,258	53,045	43,171	37,560
$W W \rightarrow q q q q$	1773.5	886,770	757,047	271,409	306
$ee W W \rightarrow ee q q q q$	464.9	282,500	269,075	150,957	23
$ev W Z \rightarrow ev q q q q$	25.5	12,770	12,271	7,033	3,696
$Z_H Z_H \rightarrow A_H A_H q q q q$	99.5	49,741	49,609	4,346	3,351
$\nu\nu W W \rightarrow \nu\nu q q q q$	6.5	3,227	3,203	2,373	1,486
Total		1,235,008	1,091,205	436,118	8,862



# Determination of $A_H$ & $W_H$ mass

Masses of  $A_H$  and  $W_H$  are determined by the edge of  $E_H$  distribution.

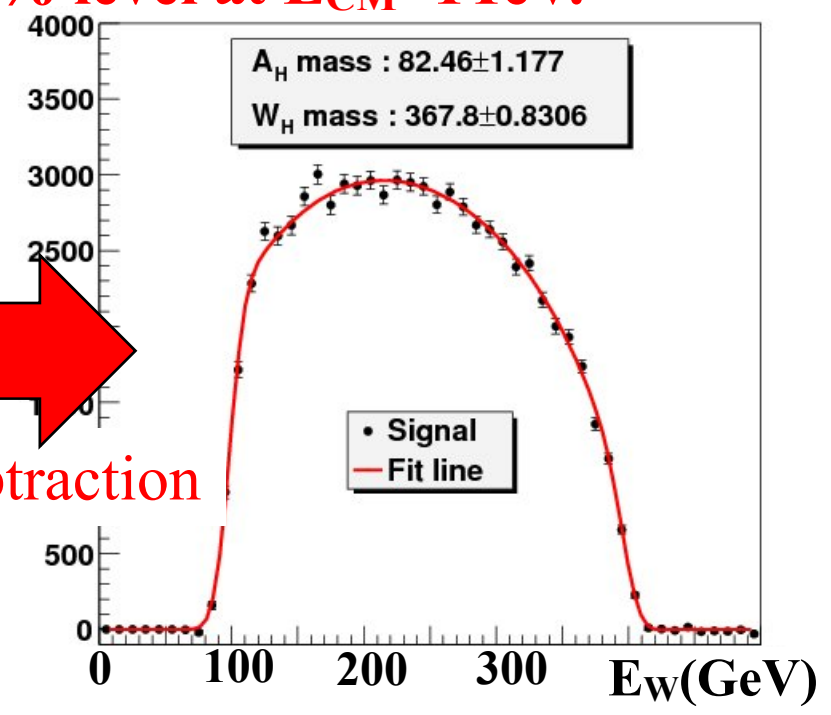
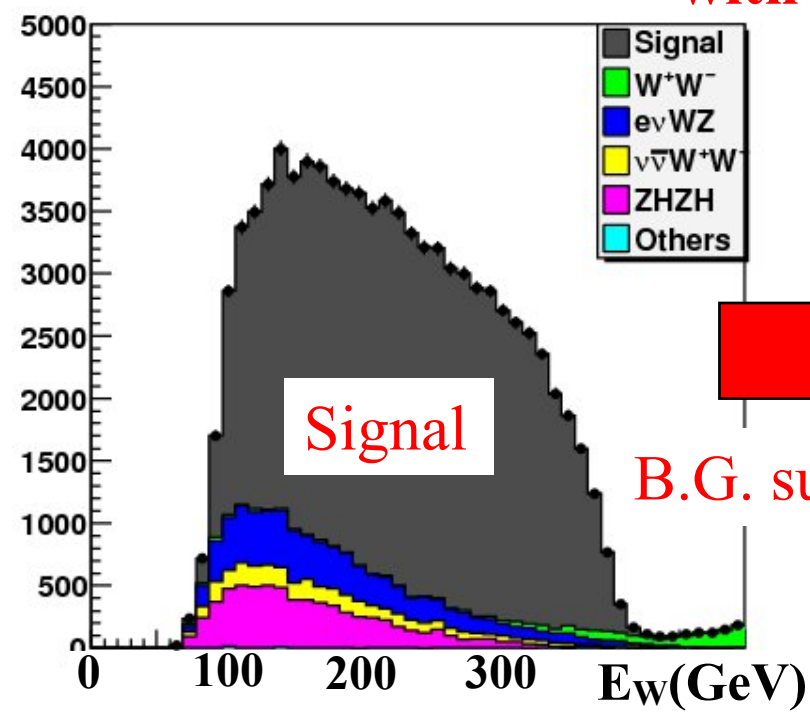
- $M_{A_H} : 82.46 \pm 1.18 \text{ GeV}$
- $M_{W_H} : 367.8 \pm 0.83 \text{ GeV}$



Measurement accuracy

- $M_{A_H} : 1.4\%$
- $M_{W_H} : 0.2\%$

**Masses of  $A_H$  and  $W_H$  can be determined with 1% level at  $E_{CM}=1\text{TeV}$ .**

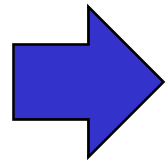


# Determination of $VEV$ & $\Omega h^2$

# Sensitivity to $VEV(f)$

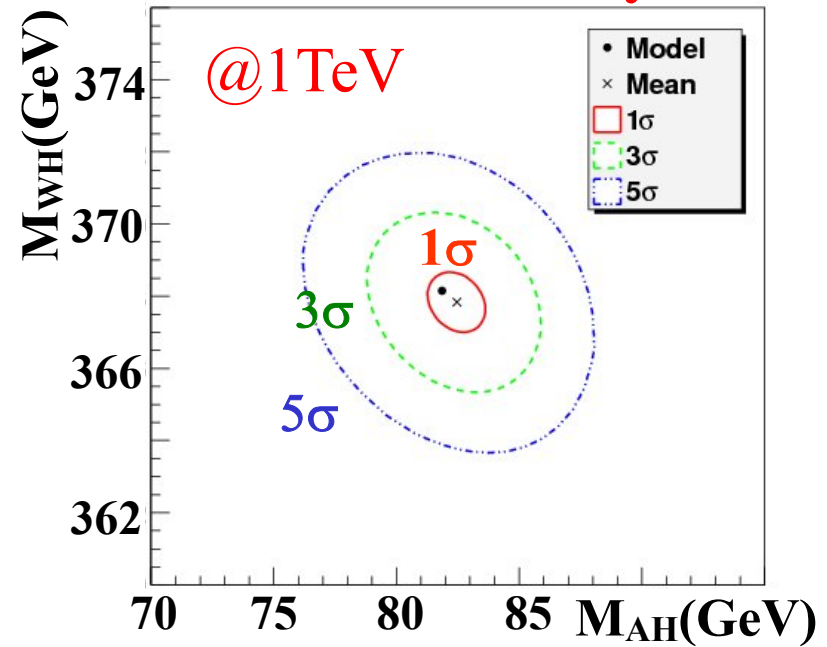
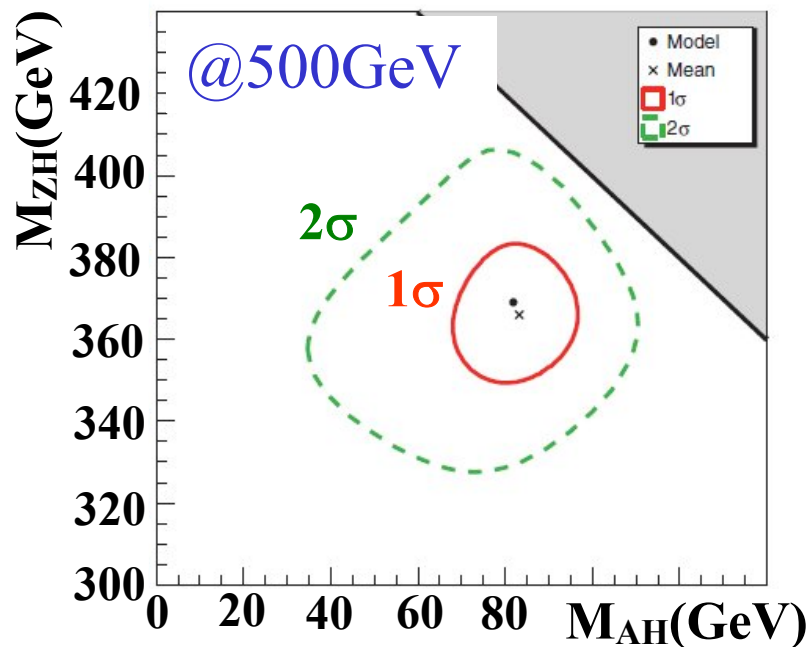
Sensitivity to  $VEV(f)$  was estimated by measurement accuracy of the heavy gauge bosons.

- $M_{AH} \sim \sqrt{0.2} g' f$ ,  $M_{ZH, WH} \sim g f$



- $f = 576.0 \pm 25.0$  (4.3%) @ 500GeV
- $f = 579.8 \pm 1.1$  (0.2%) @ 1TeV

**ILC has excellent sensitivity to  $VEV$ .**

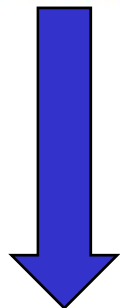


# Sensitivity to relic abundance

Finally, sensitivity to the relic abundance was investigated.

Relic abundance of  $A_H$ :

$$\Omega_{\text{DM}} h^2 = \frac{1.07 \times 10^9 x_f \text{GeV}^{-1}}{\sqrt{g_*} m_{\text{Pl}} \langle \sigma v \rangle}$$



Annihilation xsec of  $A_H$

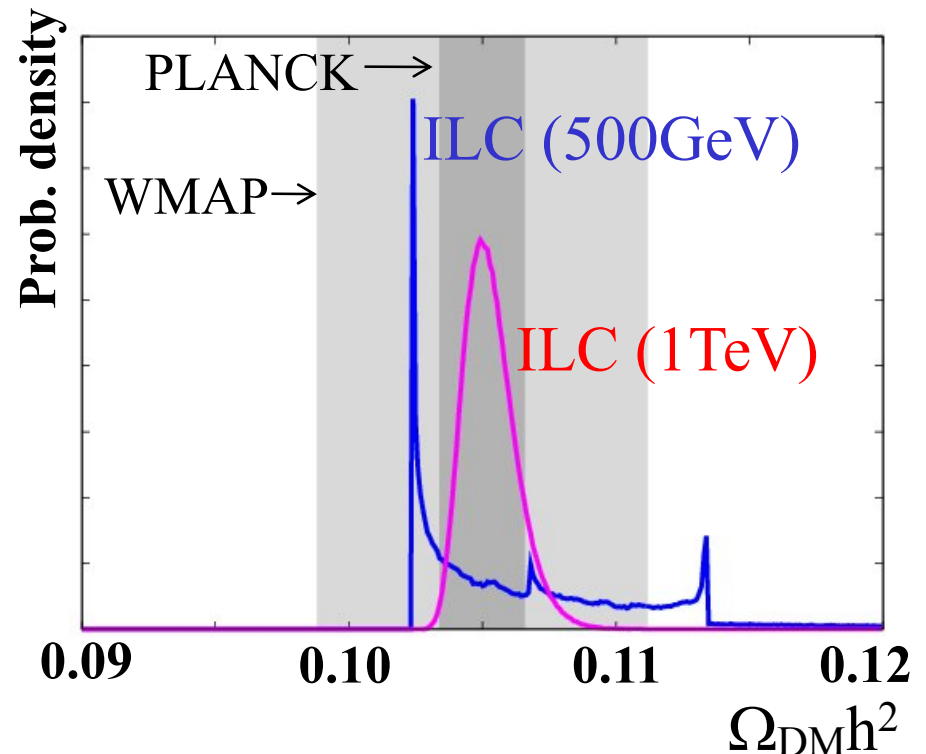
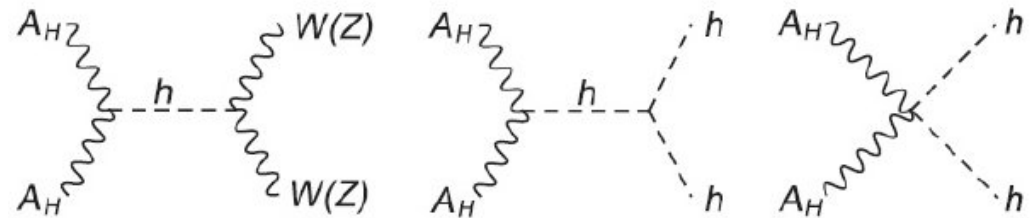
- Function of  $f$

Sensitivity to  $\Omega h^2$  depends on the measurement accuracy of  $f$ .

- $\sim 10\%$  @500GeV
- $\sim 1\%$  @1TeV

**ILC has the similar sensitivity to  $\Omega h^2$  with PLANK at  $E_{\text{CM}} = 1\text{TeV}$ .**

## Annihilation processes of $A_H$



# Summary

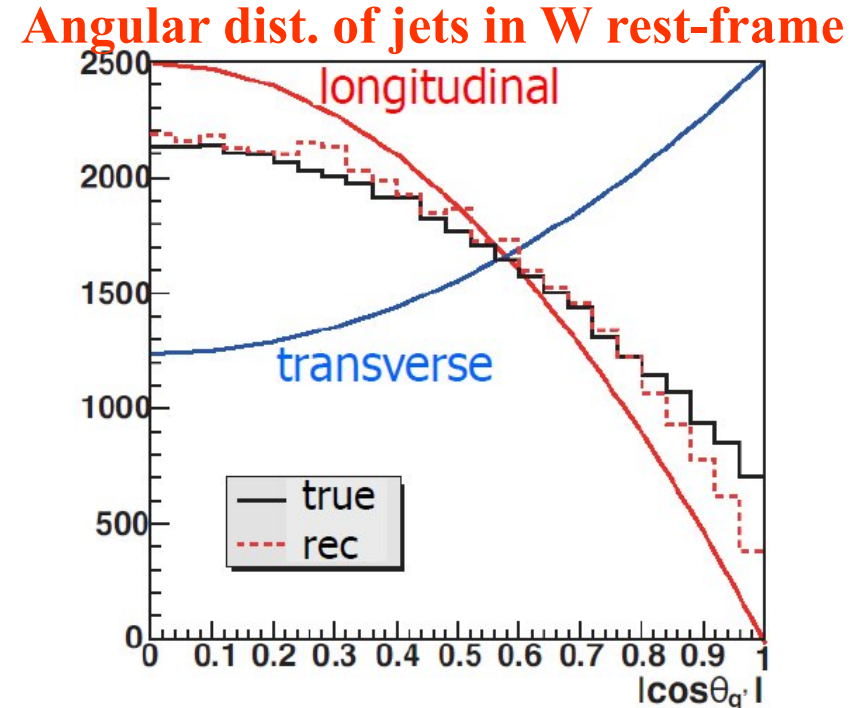
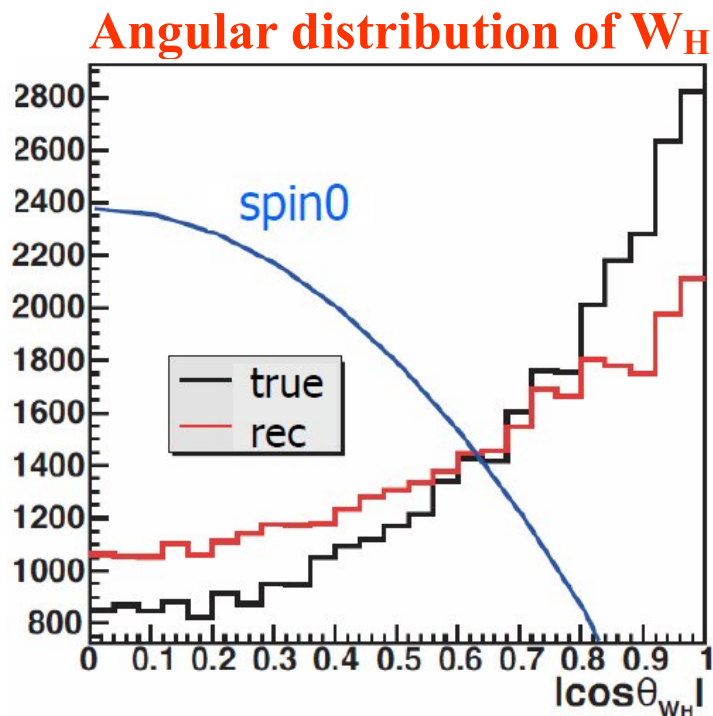
- Little Higgs model with T-parity gives solution for the little hierarchy problem.
- ILC has excellent sensitivity to the Little Higgs parameters.
  - $M_{AH}$ : 16.2%,  $M_{ZH}$ : 4.3% @ 500 GeV
  - $M_{AH}$ : 1.4%,  $M_{WH}$ : 0.2% @ 1TeV
  - VEV (f): 4.3% @500GeV, 0.2% @1TeV
- The relic abundance of  $A_H$  can be determined with the similar sensitivity of PLANK.
  - $\sim 10\%$  @ 500GeV,  $\sim 1\%$  @ 1TeV
- The paper on this study was published by PRD.
  - Phys. Rev. D79, 075013 (2009)/arXiv:0901.1081[hep-ph]





# Spin of $W_H$ & helicity of $W$

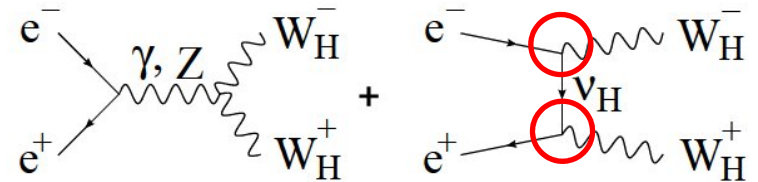
- The angular distribution of  $W_H$  is different from that of spin-0.
  - We can distinguish from spin-0 particles.
- Angular distribution of jets in  $W$  rest-frame shows the contribution of longitudinal component.
  - The coupling is confirmed to arise from the symmetry breaking.



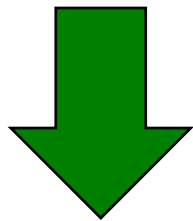
# Gauge charge of $W_H$

## $W_H$ coupling

- $W_H$  has SU(2) charge without U(1) charge.
- At high energy,  $Z \sim W^3$  almost couples to left-handed.



→  $W_H$  charge can be checked by relation of xsec. and the beam polarization.



Zero xsec. for fully right-handed polarization can be observed.

→ At ILC, we can confirm that  $W_H$  has no U(1) charge.

